Abstract

I show that the life expectancy distribution across countries is an evolving twin-peaked distribution with some countries shifting across peaks between 1962 and 1997. To draw out the implications that this has about development, I model life expectancy in terms of physical and human capital and technology, the fundamental economic variables described by economic growth theories. For concreteness, the Solow model and a convergence club growth model by Howitt and Mayer-Foulkes (2001) are used as examples. I discuss how a multiple convergence club structure can be used to define states of development and show that it must be reflected in the life expectancy dynamics. I then show by visual examination and by using mis-specification tests on levels and on convergence properties that the empirical cross-country distribution of life expectancy for the period 1962-97 is best described using a convergence club structure. This gives strong empirical evidence that only growth theories involving convergence clubs can explain the process of development.

Keywords: convergence clubs, life expectancy, economic growth, twin-peaked distribution, health
UNU World Institute for Development Economics Research (UNU/WIDER) was established by the United Nations University as its first research and training centre and started work in Helsinki, Finland in 1985. The purpose of the Institute is to undertake applied research and policy analysis on structural changes affecting the developing and transitional economies, to provide a forum for the advocacy of policies leading to robust, equitable and environmentally sustainable growth, and to promote capacity strengthening and training in the field of economic and social policy making. Its work is carried out by staff researchers and visiting scholars in Helsinki and through networks of collaborating scholars and institutions around the world.
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1. Introduction

Can ‘development’ and ‘underdevelopment’ be defined as specific economic states? Is it possible that whole sets of countries find themselves in particular types of dynamic equilibria that determine the type and extent of their growth? This is the kind of question that was addressed when development theory originated. However, the difficulties faced by development policy in practice led to the current restricted focus on poverty and on balanced macroeconomic and open, trade and investment policies. Although it is hoped that these policies will lead to growth and lift billions out of misery, they are not really based on a theory of development, but on basic general recommendations dealing with poverty and growth that in principle apply to any country.

The main reason behind this uniformity of policy is that neoclassical growth theory, on which most current policy recommendations are based, tends to consider growth to be a uniform process, leading of its own towards the convergence of income levels, particularly if policies allowing the markets to function are applied.

Recent empirical work, however, questions the neoclassical theory by stressing role that productivity differences play in explaining income differentials level between countries (Klenow and Rodriguez-Clare, 1997; Hall and Jones, 1999). Howitt and Aghion (1998) develop a theory of growth that goes beyond Solow in that it gives an endogenous account of technological change. Howitt (2000) develops a multi-country model that accounts for the endogenous nature of technological change. Howitt and Mayer-Foulkes (2001) extend this model to explain the divergence in per capita income that took place between countries during the twentieth century (documented by Pritchett, 1997), as well as the convergence that took place between the richest countries during the second half of the century. Their model implies the existence of three convergence clubs. Those in the highest club will converge to an R&D steady state, while those in the intermediate club will converge to an implementation steady state. Countries in both of these clubs will grow at the same rate in the long run, as a result of technology transfer, but inequality of per capita income between the two clubs will increase during the transition to the steady state. Countries in the lowest club will stagnate, with relative incomes that fall asymptotically to zero. Once R&D has been introduced, a country may have only a finite window of opportunity in which to introduce the institutions that support R&D, after which it will remain trapped in an implementation or stagnation equilibrium. The model implies that a series of factors known to slow growth, such as ineffective property rights, excessive taxes, weak financial and monetary institutions, corruption and lack of public services (Easterly, 2001), can determine a country’s continued permanence in a stagnation or implementation steady state. The importance of human capital as an input for both production and technological change coincides with a recent emphasis on human development.

Broadly speaking, this and other growth models with multiple steady states—and therefore convergence clubs—present a paradigm allowing for the definition of states of development. In the Howitt and Mayer-Foulkes (2001) model developed countries are those carrying out R&D, and there are two kinds of underdeveloped countries: those implementing current technological advances and those in stagnation. Finer subdivisions are possible with models incorporating other relevant economic phenomena such as trade,  

1 The first version of the paper can be accessed from http://www.nber.org/~confer/2001/si2001/efbdprg.html
or other sources of multiple steady states, for instance in human capital dynamics (Azariadis and Drazen, 1990; Benabou, 1996; Durlauf, 1993, 1996; Galor and Zeira, 1993; Galor and Tsiddon, 1997; Tsiddon, 1992). Specific health phenomena leading to convergence clubs may also be involved. To begin with the efficiency theory of wages (e.g. Dasgupta and Ray, 1986; Dasgupta, 1991) implies the possibility of a low productivity, low nutrition trap. An intergenerational low educational and low health and nutrition trap is also possible (Galor and Mayer-Foulkes, 2002), and may be faced once some minimal level of nutrition is achieved. This trap may also be an ingredient for a low technology trap.

In the language of dynamics, countries can be defined to be in a specific state of development if their growth dynamics lie in the basin of attraction of a specific configuration of economic of growth. Conversely, empirical evidence that growth dynamics posses convergence clubs implies that growth is occurring though a process involving multiple steady states. A fuller knowledge of the underlying economics can lead to policies specifically aimed at dissolving technological and other growth traps and therefore at changing states of development.

A budding literature exists on convergence clubs. In cross-country studies of income distribution dynamics, Quah (1996, 1997) finds little convergence. Instead, he finds persistence, immobility, polarization and an emerging twin-peaked income distribution since the 1980’s. Here, we find twin peaks in the life expectancy distribution since 1962, implying that a preexisting convergence club structure may be the antecedent for the divergence in incomes found by Quah. The changing twin peaked structure found here is more specific than but not inconsistent with the “emerging twin peaks”. Desdoigts (1999) finds cross-country evidence for a non-linear association of higher stages of development with higher stages of growth. Engelbrecht and Kelsen (1999) find that the APEC countries have distinct convergence properties from the OECD and European Union groups of economies. Andrés and Bosca (2000) find evidence for convergence clubs within the OECD. There are also some country specific studies showing, for instance that Ireland (O'Rourke and Grada, 1994) and New Zealand (Greasley and Oxley, 2000) do not grow as well as groups of countries thought to be their natural convergence partners.

Convergence clubs may be at the root of the evolution of income inequality, because most income inequality is between countries and thus depends on relative growth (Quah, 2001), and growth in turn tends to increase incomes within country proportionally (Dollar and Kraay, 2001a, 2001b).

Establishing the existence of convergence clubs empirically may thus play a crucial role in understanding the problems and setting out the appropriate policies for development. The purpose of this paper is twofold: 1) To establish the existence of three large scale convergence clubs in life expectancy dynamics during the period 1962-97 and 2) to show that only growth theories with multiple steady state are consistent with these life expectancy dynamics. To do this I first show that life expectancy dynamics can be modeled using the theories of economic growth, and that they must reflect the convergence club structure of any underlying theory. Then I show that the data supports the existence of at least three large-scale convergence clubs. The first has very low levels of life expectancy to this day and thus roughly corresponds to the concept of stagnating countries. The second had very low levels of life expectancy in 1962, which nevertheless rose quickly and thus consists of countries implementing basic technologies for the population as a whole. The
third consists of countries that already had relatively high life expectancies in 1962. This includes the developed and a top layer of underdeveloped countries and still invites further subdivision into an R&D and a second implementation club at a higher technological level. This is carried out in Mayer-Foulkes (2002).

Life expectancy is one of the best widely available indicators of population welfare. In fact, its five–yearly data is more complete than that for either income or education. Life expectancy results from the general availability of private and public goods and services covering basic needs and providing the technological inputs and social organization for health. Since freedom from disease and premature death are amongst the main human aims at both the individual and social levels (Sen, 1999), life expectancy attainment is an excellent indicator of population-wide development. Its importance has been recognized by its inclusion in the Human Development Index (also including education and income).

Recent research has found that the links between life expectancy and income are indeed very close. In a cross-country study, Preston (1975) showed that life expectancy is positively correlated with income, with higher levels of life expectancy achieved for equivalent levels of income in later periods. Pritchett and Summers (1996) carefully corroborate by means of instrumental variable techniques that countries with higher incomes enjoy higher health, suggesting, as Anand and Ravallion (1993) find, that the main causal channels of this relationship are the income levels of the poor and public expenditure in health care. There is also a causal relation from health to income. Fogel (1994) finds that increased nutrition and health account for up to a third of the economic growth in Great Britain during the last 200 years. Macroeconomic studies of economic growth such as Barro’s (1991) have found life expectancy to be an important predictor of economic growth. In more recent work, Mayer-Foulkes (2001) shows that health indicators are associated with a long-term impact on economic growth in Latin America during the period 1950-90. Arora (2001) finds cointegration between economic growth and health in 100-125 year time series for seven advanced countries, with growth responding to the changes in health and not vice versa. There has also been intense microeconomic research on the role of health and nutrition investment and returns (Schultz, 1992, 1997, 1999, Thomas, Schoeni and Strauss, 1997; Strauss and Thomas, 1998; Savedoff and Schultz, 2000, amongst many others), although the magnitudes found for the health impacts tend to be smaller than those measured macroeconomically. Height and weight, as indicators of population health, have been established as standard of living indicators that rival aggregate measures of income (e.g. Steckel, 1995). These are well known to be causally interlinked with life expectancy (Fogel, 1994).

Life expectancy is thus an excellent measure of the standard of living. As a measure of population welfare it is probably better than income. It is more sensitive to inequality (the longevity of the rich is less than proportional to their wealth), and its production requires, in addition to capital, a richer mix of public services and technology. In contrast, important proportions of the income of many underdeveloped countries have tended to be associated with a small number of sectors applying a limited spectrum of technologies. Health may thus index the fundamentals of development better than income per capita, explaining why the macroeconomic causal impact of health indicators on income is found to be larger than

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2 Only 24.4 percent of the countries that will be classified below as having low life expectancy in 1962 were classified by the 1990s as diversified exporters in the World Bank data base refered to below.
the corresponding microeconomic relationships. Health measures are also closely correlated with education (Savedoff and Schultz, 2000; Schultz 1997, 1999) and thus are good indicators of human development, an ever more important ingredient for productivity. Besides this, data for health is available for many more countries over longer periods than data for income. This provides an opportunity for testing economic growth models by using health data.

Figure 1
Cross-Country Life Expectancy Histograms, 1962-97
Based on the close association of health with income and growth, I take the theoretical viewpoint, in the cross-country context, that life expectancy can be modeled in terms of the theories of economic growth. I model health as a function of the main underlying economic variables, namely capital and technology, much like income is. For concrete examples I use both the Solow (1957) model and the Howitt and Mayer-Foulkes (2001) endogenous technology convergence club model. Expressed in these models as a function of capital per capita and technology, life expectancy thus provides an indirect measure of the underlying variables. It will follow that when an economy converges to a steady state, life expectancy will converge to a corresponding trajectory, and that if several steady states exist, then several such life expectancy trajectories will exist. In addition, if relative convergence holds among economies tending to the same steady state, life expectancy will inherit the same property. Thus, each of these two theories of growth, as well as any other to which life expectancy could be similarly added, predicts a qualitative property of life expectancy dynamics. The Solow model predicts a single convergence club, while the Howitt and Mayer-Foulkes model predicts multiple convergence clubs. Thus, testing life expectancy dynamics for convergence clubs is in effect a test of the qualitative predictions of these growth models. Finding that life expectancy dynamics exhibit convergence clubs implies that only growth models predicting convergence clubs can hold.

Our qualitative test of the Solow and Howitt and Mayer-Foulkes models (which applies to most growth models) thus consists of a test of the descriptive properties of life expectancy dynamics.

The empirical study uses the cross-country life expectancy database by Easterly and Sewadeh that is available on the World Bank web page. A complete five-yearly panel is available for the period 1962-97 for 159 countries. I first invite the reader to a visual examination of the life expectancy histograms for each of the years in the panel. A changing two-peaked pattern is clearly apparent. In 1962, half of the countries formed a low peak and the other half a high peak. By 1997, half of the countries in the low peak had migrated to the high peak, and the peak structure had shifted about 5 years to the right along the life expectancy axis (Figure 1). On the basis of these histograms I define three sets of countries, according to their life expectancy trajectories: ‘Low-Low’ (LL), ‘Low-High’ (LH), ‘High-High’ (HH). I then propose these three sets as possible convergence clubs and proceed to analyze the trajectories’ levels and their convergence properties. First I show by means of a series of summary statistics and graphs that this subdivision reflects different development processes, and does not result from multi-peakedness of the birth rate, an important parameter in growth models. To analyze the levels we show, using and F-test applied to quadratic estimates of log life expectancy, that a three clubs model is much better than the single club model. To analyze the convergence properties I use F-tests to show that three clubs models for both levels and life expectancy change fit the data better than single club models. The visual and statistical examination of the data clearly shows that the process of life expectancy improvement in these three groups of countries was quite different, and that each subdivision of the sample enjoys the properties of a convergence club. Section 2 contains the theory, Section 3 the empirical work, and Section 4 the conclusions.

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3 The address is http://www.worldbank.org/research/growth/GDNdata.htm
2. Growth theories and life expectancy

As was mentioned above, there is strong evidence that life expectancy rises with income, and that, as a result of technological progress, higher life expectancies have been obtained at later dates for the same income. Besides, there is evidence that health itself increases productivity, through a series of mechanisms including increased labor, educational and household productivity, and female economic participation. This and other research on health has led to the concept of health capital as an extension of human capital mainly consisting of education (see for example Savedoff and Schultz, 2000).

For our Solow model, we may broaden the notion of capital to include physical, human and health capital. We can then write the Solow model of economic growth with exogenous technological change for each country as:

\[ k' = s\Phi k^\alpha - (n + \delta + g)k, \]  
\[ A_{World}' = g A_{Worlds}, \]  

where \( k \) is capital per effective worker, \( s \) is the saving rate, \( \Phi \) is a country-specific fixed productivity factor, \( \alpha \) is the elasticity of a Cobb-Douglass production function, \( n \) is the population growth rate, \( \delta \) is the depreciation rate and \( g \) is the rate of growth of \( A_{World} \), the globally available level of technology. We now suppose that health (which shall be measured by life expectancy) is given by

\[ v = \Psi k^\theta A^\phi \]  

(\( v \) for vitality), where \( \theta \geq 0, \phi \geq 0 \) and \( \theta + \phi < 1 \) to obtain the property that life expectancy increases less than proportionally to income. This expression includes the idea that health depends on the consumption stream and also that capital and technology are among the main inputs for health. \( \Psi \) represents a country-specific factor expressing how much health is produced at given levels of capital and technology. It includes such factors as preferences for health, inequities in the distribution of income, and the equity, level and efficiency of public policy. Note that income is given by \( Ak^\alpha \), so that \( v \) can be viewed as partly or wholly a function of income, according to the reader’s preferences. The expression for \( v \) would arise under Cobb-Douglass preferences if these imply that a constant proportion of income is spent on health and if health is a homogeneous function of order \( \theta + \phi \) of expenditure on health.

The Howitt and Mayer-Foulkes model is based on the premise that a new method for creating technological change, ‘research and development,’ was introduced early in the twentieth century. In order to take advantage of this method a country must have (i) an appropriate set of supporting institutions and (ii) at least a threshold level of human capital that depends on the technological frontier. Countries that do not fulfill both of these requirements can only create new technologies through an older method, ‘implementation.’ Here I do not report the fairly complex framework used to model technological change, but only state the closed form equations that hold about each steady state:5

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4 This assumption is necessary to obtain convergence equation (11).

5 I follow the model in the first version of the paper, which can be found at the above mentioned website or at http://www.cide.edu/investigadores/David_M/HomePage.htm
\[ h' = s \Phi h^\beta - (n + \delta + \pi_r(\psi, h, \lambda)(a^{-1} - 1))h, \quad (4) \]

\[ a' = \pi_r(\psi, h, \lambda)(1-a) - a \gamma \text{World}, \quad (5) \]

where \( h \) is human capital per effective worker, \( \psi \) is a country-specific index for the incentives to innovation, \( \pi_r(h, \lambda) \) is the intensity of successful innovation, an increasing function of \( \psi \), \( h \) and of \( \lambda \), the productivity of the innovation technology characterizing the stationary state, either R&D or implementation. If the incentives for innovation are too small, as in the case for stagnation, \( \pi \) may be negative and is replaced by \( \pi_r = \max[\pi_r, 0] \). In this model \( a = A/A \text{World} \) is the relative technological level of each country, defined with respect to the global leading edge technological parameter \( A \text{World} \). \( A \) is the average technological level of the intermediate goods industries. \( A \text{World} \) is the maximum of the country-specific \( A \)'s and grows at a rate \( g \text{World} \) given by the technological spillovers of worldwide innovation through R&D and implementation. As mentioned above, R&D is possible only if the per capita level of human capital is above a certain threshold that rises with the leading technological edge \( A \text{Max} \). Thus the productivity of innovation is

\[ \lambda = \lambda_{R&D} \text{ for } ha \geq \eta, \text{ and } \lambda = \lambda_{Imp} \text{ for } ha < \eta, \quad (6) \]

where \( \eta \) is the innovation effective human capital threshold and \( \lambda_{R&D} > \lambda_{Imp} \), stating that innovation is more productive through R&D than through implementation.

We suppose as before that health is given by

\[ v = \Psi h^\theta A^\phi. \quad (7) \]

Physical capital, which has been excluded for simplicity, can be added to this model. The convergence club structure is retained, although steady state levels may depend on whether the economy is open or closed. Note that equation (1) in the Solow model is analogous to equation (4) in the Howitt and Mayer-Foulkes model, with the rate of technological growth replaced by the endogenous rate \( \pi_r(\psi, h, \lambda)(a^{-1} - 1) \).

Each of the steady states of these two models (and generically those of any steady state of any model) has the property that as trajectories approach the steady states they do so at an exponential rate given by the absolute value of some largest eigenvalue, \( -\mu \), which is negative, depends on the parameters of the model and may be steady-state specific. Using the same arguments as Barro and Sala i Martin (1990), a log-linearization at each steady state implies that the normalization

\[ \nu = \nu/(A \text{World})^\phi = \Psi h^\theta a^\phi \text{ or } \Psi k^\theta a^\phi \quad (8) \]

converges exponentially to its steady state \( \nu^* \). Hence

\[ \log[\nu(t)] = \log[\nu(0)] \exp(-\mu t) + \log(\nu^*) [1-\exp(-\mu t)]. \quad (9) \]

This implies that the non-normalized quantity \( \nu \) satisfies
\( (1/T) \log[v(t+T)/v(t)] = \varphi g + (1/T) [1-\exp(-\mu T)] [\log(v^*)-\log(v(t))] \)  
\[ (10) \]

\[ = \varphi g + (1/T) [1-\exp(-\mu T)] [\log(v^*)-\{\log(v(t)) + \varphi \log(A_{World}(0)) + \varphi gt\}] \]. \[ (11) \]

(with g replaced by \( g_{World} \) in the case of the Howitt and Mayer-Foulkes model). This is the basic equation describing relative convergence that we estimate. The convergence coefficient is \(-(1/T)[1-\exp(-\mu t)]\). A term involving time appears because of the dependence of \( v \) on the leading technological edge. This equation would be satisfied by life expectancy \( v \) generically near any steady state of any model including capital or human capital also modeling \( v \) though equation (3) and (7).

In expression (11) \( v^* \) is an unknown quantity that depends on the parameters \( s, \Phi, \alpha \) or \( \beta, n, \delta, \Psi, \theta, \varphi, \psi, \lambda \) and \( g \) or \( g_{World} \). \( \lambda \) is a steady state specific parameter, while \( g \) and \( g_{World} \) are global parameters. The technology parameters \( \alpha, \beta, \theta, \varphi, \delta \) are usually thought of as global. The remaining parameters \( s, \Phi, n, \Psi, \psi \) are country-specific. Through the term including the steady state level \( v^* \), they give rise to fixed effects reflecting different conditions in each country. It is found below that under three clubs models the fixed effects have single-peaked distributions for each proposed convergence club. On the other hand, they have multiple peaked distributions under single club models. It is verified separately that the distribution of the population growth rate \( n \) is single-peaked. Thus the three clubs models are consistent with the point of view that the multiple-peakedness of life expectancy is an overriding economic phenomenon. By contrast, for the single club models, the multiple peakedness of the fixed effects remains to be explained and would have to arise from institutional or economic policy considerations, or other reasons even further afield from economics.

Equation (11) is steady-state specific. If data from several steady states are pooled together, the resulting convergence coefficient will still be negative. If a data set is partitioned into several subsamples, a better estimate of equation (11) may result if the subsamples contain countries belonging to different steady states for which equation (11) has different coefficients. However, the boundaries of these subsamples may be imprecise and further subdivision may still be possible. Note that when referring to relative convergence the assumption of a single club is usually made. Here I am explicit about the number of clubs and regard relative convergence as a club-specific property.

We now have as examples two models of life expectancy based on the dynamics of the fundamental economic variables, as given by the Solow or the Howitt and Mayer-Foulkes models of economic growth. Life expectancy works as an indicator of each country’s economic state. It is quite clear that the arguments above are applicable to most if not all other dynamic models of capital and technology. Ramsey type growth models lead to convergence equations such as (11). Two-sector models with physical capital and human capital (representing knowledge rather than skill) also exhibit convergence to their steady states, so that life expectancy expressed as a function of capital and knowledge would similarly converge to a steady state trajectory.

Indicators functions (in this case life expectancy) have been used to study chaotic dynamics, because generically they contain all of the information on the qualitative properties of the dynamical system. This is the content of Taken’s theorem, which applied
in this context to discrete models of economic growth says the following: Generically, the
dynamics of any attractor of any m-dimensional growth model will be qualitatively
reproduced by the dynamics of m-histories of life expectancy \( (LE_{t-(m-1)\tau},...,LE_t) \), for any lag \( \tau \).

Thus the model for the convergence of life expectancy to one or to several steady states
according to an underlying theory of economic growth, is quite general and gives rise to a
formal test of the qualitative properties growth models must have to be consistent with the
descriptive properties of life expectancy dynamics. I concentrate on comparing the
hypothesis that there is a single or that there are several convergence clubs, each
possessing the property of relative convergence. In the examination of life expectancy
dynamics I find that ignoring the existence of a club structure either in a description of the
levels or in a relative convergence test, involves a significant specification error that is
detected by omitted variables tests, and a failure to explain the multiple peakedness of
fixed effects.

3. Empirical dynamics of life expectancy

The life expectancy data consists of a five-yearly panel of data over the period 1962-97
that is complete for 159 countries, available on the World Bank web page mentioned
above. By comparison, the 1960-95 GNP panel is complete for only 122 countries; even
less educational data is available.

I conduct the descriptive study of this data as follows. First I examine the five-yearly
histograms for life expectancy. These clearly exhibit a changing twin-peaked structure with
three groups of countries: those originally in the high peak (HH), those originally in the
low peak shifting to the high peak (LH) and those remaining in the low peak (LL). The
histograms also exhibit a slow shift towards higher life expectancy.

The dynamic structure that the histograms exhibit thus gives rise to a subdivision of
countries into three groups, LL, LH and HH. I next give additional evidence by means of
several summary statistics that this subdivision distinguishes between different types of
dynamics, and that it is not unduly influenced by the population growth rate.

Finally, I examine the levels and the convergence properties followed by life expectancy
dynamics, to see to what extent these slow and fast moving peaks correspond to
convergence clubs.

3.1 Life expectancy histograms

Figure 1 shows the distribution of life expectancy across the 159 countries for which a
balanced panel is available. In 1962 and 1997 these histograms have a well-defined twin-
peaked structure. However, the size of these peaks is different. As can be ascertained by
observing the full sequence of histograms, a group of countries has traveled from the lower
to the higher peak. Also, both peaks have shifted about five years to the right. In 1962
about half the countries in the sample were in the lower peak. The median life expectancy
of 54.865 years lies right in between the two peaks. By 1997 about half of the countries in the lower peak had moved beyond this reference level.\textsuperscript{6}

The histogram motivates the definition of the subsamples LL, LH and HH as follows. LL is the set of countries with life expectancy less than the median 54.865 in 1962 and also less than this level in 1997. LH are those countries that were below this level in 1962 and above it in 1997. The HH countries were above this level at both dates. Table 1 shows the composition of the three subsamples by regions.

Figure 2 shows a ±3 standard deviation band for the estimated mean log life expectancy of each subsample (transformed back into years).\textsuperscript{7} The results confirm the life expectancy trends of the three subsamples that are visually evident in the sequence of histograms.

Examination of these groups shows that the LL countries are located mainly in Sub Saharan Africa. HH includes Europe and North America as well as 13 countries in East Asia Pacific and 21 countries in Latin America and the Caribbean (thus picking up the developed world as well as an upper layer of underdeveloped countries). LH countries include the rest of the underdeveloped world.

The mean life expectancy for LL countries is 39.5 in 1962, rising to 48.2 by 1997. These countries had very low income and technology levels in the sixties, improving only very slowly through the thirty-five year period. LH countries improved much more rapidly from an initial 46.9 to 64.6 years of life expectancy. The initial life expectancy is still at a very low level corresponding to low income and technology levels, but the final level can only be attained on the basis of sufficient private and public health inputs. HH countries improved from 65.4 to 74.1 years, indicating a high technological level throughout.

\textsuperscript{6} Visual examination, as well as subdivision of the intervals, confirms that these features are robust to the choice of life expectancy intervals.

\textsuperscript{7} The means are estimated by regressing against a constant for each time period.
3.2 Some issues on the choice of subsamples

Changes in life expectancy over the period 1962-97 can be seen in Figure 3, which examines these changes by countries and by continents, and also shows where the LL, LH and HH subsamples lie. It is quite clear that the full sample does not consist of a simple single-humped distribution. I have not attempted to subdivide the HH group into convergence clubs, considering that other data or methods may be required. Before examining the dynamics of these subsamples we discuss some issues regarding their choice.8

The division of the sample of countries into low and high life expectancy groups in 1962 is not too arbitrary because the distribution is double-peaked and the median lies right in between the peaks, especially as shown in a more finely subdivided histogram. On the other hand the boundaries between the LL and LH groups may seem somewhat arbitrary. It may appear that its choice introduces selection bias in the level analysis, because these groups are defined on the basis of their ex-post performance in life expectancy improvement. However, the main point is that the life expectancy of countries starting at a low level diverges. Figures 4.1 and 4.2 show the life expectancy histograms for the LL and LH groups in 1962 and 1997. The two distributions clearly diverge, something that does not depend on the exact location of the boundary. If anything, some of the lower LH countries should be classified as LL countries, making the divergence between the two subsamples even larger. Further evidence of the differences between the samples is found in Figures 5.1 and 5.2, which show the average evolution of life expectancy for the full sample and for the three subsamples.10 Figure 5.1 shows that life expectancy

8 The histograms in Figure 1 portray a balanced sample of 159 countries. For the regressions I was slightly less stringent and included all countries for which data was available in 1962 and 1997. This added four countries that were missing a single data point (subsample and year in parentheses): China (LH, 1977), Hungary (HH, 1977), Japan (HH, 1977) and Turkmenistan (HH, 1992). The full subsamples are the following:


High-High: Albania, Argentina, Armenia, Australia, Austria, Azerbaijan, Bahamas, Bahrain, Barbados, Belarus, Belgium, Brazil, Bosnia and Herzegovina, Brunei, Bulgaria, Canada, Chile, Colombia, Costa Rica, Cuba, Cyprus, Denmark, Estonia, Fiji, Finland, France, Germany, Greece, Guadeloupe, Guyana, Hong Kong, Hungary, Iceland, Ireland, Israel, Italy, Jamaica, Japan, Dem. Rep. Korea, Rep. Korea, Kuwait, Latvia, Lebanon, Lithuania, Luxembourg, Macao, Malaysia, Malta, Martinique, Mauritius, Mexico, Netherlands, Netherlands Antilles, New Caledonia, New Zealand, Norway, Panama, Paraguay, Poland, Portugal, Puerto Rico, Qatar, Reunion, Romania, Singapore, Slovenia, Spain, Sri Lanka, Suriname, Sweden, Switzerland, Taiwan, Tajikistan, Trinidad and Tobago, Turkmenistan, Ukraine, United Arab Emirates, United Kingdom, United States, Uruguay, Venezuela and Yugoslavia (Serbia/Montenegro).

9 See also the level regressions and Figure 2.

10 Figure 5.2 is in logarithms so as to correspond with the convergence estimates.
improvements have diminished through the years. However, as can be seen in Figure 5.2, this cannot be explained simply by diminishing returns to expenditure in health. For example, LH countries improved their life expectancy more in 1962-67 than LL countries did in 1992-97 at very similar life expectancy levels, even after 30 years of technological improvements! It is also apparent that the experience of each group of countries does not lie in the neighborhood of the average cross-country performance.
Another issue that must be considered is whether the distribution of population growth may be behind the several-peaked nature of the full sample. However, as can be seen in Figure 6, the distribution of population growth was single-peaked in 1960. A growing number of countries experienced low population growths, but mostly in the HH group (Figures 7.1 and 7.2). Figure 7.1 shows that the population growth histogram for the HH countries was twin-peaked, a piece of evidence for the existence of convergence clubs within this subsample. However, the distributions for the LL and LH countries are not very different, so that they do not originate the distinction between these groups. Nevertheless, the demographic transition was more advanced in the LH countries: they had a higher population growth in 1960 (which would imply slower economic growth!) and a lower one in 1997, confirming that these groups of countries were indeed on different development trajectories.

Figure 5
Life expectancy dynamics 1962-97
5.1 Average changes in life expectancy 5.2 Phase diagram for sample and subsamples for sample and subsamples

It is clear that life expectancy and the population growth rate were not direct determinants of the divergence between the LL and LH groups noted above. Suppose that these groups of countries correspond to convergence clubs. According to the Howitt and Mayer-Foulkes (2001) model, the most likely determinant of membership would be the initial levels of capital and technology, because the human capital level, as indicated by life expectancy, is similar. Fixed factors such as institutional quality, productivity and incentives to innovation may affect membership, but countries similar in these respects may nevertheless belong to different convergence clubs for reasons lying in the past. I show with a probit regression some correlates of whether a country belonged to the LH rather than the LL group. The probit regression, run on the LL and LH countries, is the following (z-statistics in parenthesis):11

11 $I_{LH}$ is an indicator function equal to 1 for LH and 0 for LL countries. LE1962, SECONDARY1960, URBAN1960, RGDP1960 and N1960 are life expectancy, the proportion of secondary school enrolment and
\[ I_{LH} = -42.06 + 9.677 \log(LE1962) + 1.608 \text{(SECONDARY1960 > 5\%)} + \]
\[ (-2.648) \quad (2.386) \quad (2.637) \]
\[ -0.010 \text{URBAN1960} + 1.112 \log(RGDP1960) - 1.879 N1960 \]
\[ (-0.376) \quad (1.817) \quad (-1.818) \]

The significant indicators (all at better than 7 percent) of belonging to LH rather than LL all reflect levels of physical and human capital and technology, except for the population growth rate, which appears as well.\(^{12}\)
8.1 Single club AR(1) level model
8.2 Three club AR(1) level model

8.3 Single club relative convergence model
8.4 Three club relative convergence model (strict)

3.3 One or several convergence clubs: levels

I now test whether the life expectancy dynamics are better modelled by taking the three groups of countries as clubs than by considering the full sample as the only club. I use a descriptive quadratic model in time to look at the paths followed by the trajectories. Since life expectancy within countries is persistent, its initial level has a long-term impact and its disturbances are positively serially correlated. Therefore I use a fixed effects model and an autoregressive error structure. Both features were confirmed to be significant. In the presence of convergence clubs, each club’s trajectory is expected to have distinct levels and parameters across time. The single club model is the following:

*Model L1. Single Club:*
Index \( i \) runs through the sample of countries while \( t \) takes de values 1962 to 1997 in five yearly increments. \( \text{TIME}_t \) is measured in quinquenia from 1 to 7. The club structure is modeled by choosing different quadratic expressions for each club. The three club model is the following:

**Model L2. Three Clubs:**

\[
\log(LE_{it}) = a_i + (c_1LL + c_2LH + c_3HH)\text{TIME}_t + (c_4LL + c_5LH + c_6HH)\text{TIME}^2_t + u_{it}
\]

LL, LH and HH are dummies for the groups of countries selected above. Since life expectancy changes are persistent, it is to be expected that the errors \( u_{it} \) show a positive serial correlation. This is confirmed by the Durbin-Watson statistic when the panel is estimated without autoregressive errors. The autoregressive error structure used to estimate level models L1 and L2 is:

\[
u_{it+5} = \rho u_{it} + \epsilon_{it}
\]

The White heteroskedasticity correction is applied, because regressions of squared OLS residuals showed significant correlation with quadratic expressions of the independent variables. It yields the more conservative estimates.

The results are shown in Table 2. The coefficients of all terms containing \( \text{TIME}_t \) (respectively \( \text{TIME}^2_t \)) are significant and positive (respectively negative) as expected. An F statistic of 22.6 (yielding a p value of zero) shows that the three club is significantly better than the single club model.\(^{13}\) Wald tests show that the coefficients describing the LL group of countries are significantly different from those describing the LH or HH groups. The Durbin-Watson test shows that no further significant autocorrelation exists in the AR(1) models.

Figures 8.1 and 8.2 show the fixed effects by groups of countries for the single and three club level models. In the case of the three club model the fixed effects are graphed with origin set at the club specific averages of 30.3, 38.7 and 59.7 years. Once these averages are removed the distribution of fixed effects is similar across groups of countries, although there is less dispersion in the HH group.

### 3.4 One or several convergence clubs: relative convergence

I estimate the following relative convergence models, each based on equation (11). It is worth noting that since what is under examination is a *descriptive* feature, the problem of

\(^{13}\) To conduct these tests, LL was substituted with 1 in Model L2. The hypothesis that the coefficients of the variables containing LH and HH are all zero was then tested.
endogeneity does not arise. On the other hand, heterogeneity in the form of clubs is precisely what is being tested. Note that in the presence of convergence clubs, differences in the convergence coefficients may be expected but need not occur.

**Model RC1. Single Club:**

\[
(1/5)(\log(\text{LE}_{i,t+5}) - \log(\text{LE}_{i,t})) = a_i + c_1 \text{TIME}_t + \beta \log(\text{LE}_t) + u_{i,t}
\]

**Model RC2. Strict Three Club:**

\[
(1/5)(\log(\text{LE}_{i,t+5}) - \log(\text{LE}_{i,t})) = a_i + c_1 \text{TIME}_t + \\
+ (\beta_{LL} + \beta_{LH} + \beta_{HH}) \log(\text{LE}_t) + u_{i,t}
\]

**Model RC3. Lax Three Club:**

\[
(1/5)(\log(\text{LE}_{i,t+5}) - \log(\text{LE}_{i,t})) = a_i + (c_1LL + c_2LH + c_3HH) \text{TIME}_t + \\
+ (\beta_{LL} + \beta_{LH} + \beta_{HH}) \log(\text{LE}_t) + u_{i,t}
\]

**Model RC4. Parsimonious Strict Three Club:**

\[
(1/5)(\log(\text{LE}_{i,t+5}) - \log(\text{LE}_{i,t})) = (a_{LL} + a_{LH} + a_{HH}) + c_1 \text{TIME}_t + (\beta_{LL} + \beta_{LH} + \beta_{HH}) \log(\text{LE}_t) + u_{i,t}
\]

**Model RC5. Parsimonious Lax Three Club:**

\[
(1/5)(\log(\text{LE}_{i,t+5}) - \log(\text{LE}_{i,t})) = (a_{LL} + a_{LH} + a_{HH}) + (c_1LL + c_2LH + c_3HH) \text{TIME}_t + (\beta_{LL} + \beta_{LH} + \beta_{HH}) \log(\text{LE}_t) + u_{i,t}
\]

These models estimate convergence equation (11). The fixed effects \(a_i\) correspond to the country-specific steady state levels \(v^*\), together with the constant \(\phi_g\). The single club convergence coefficient in model RC1 is \(\beta\) while the club specific convergence coefficients in the three club models RC2 and RC3 are \(\beta_{LL}\), \(\beta_{LH}\) and \(\beta_{HH}\). The transformation between life expectancy \(v\) and technology corrected life expectancy \(\tilde{v}\) (equation 8) may be somewhat arbitrary. This is why the lax three club model RC3 allowing club-specific time coefficients is proposed. In the parsimonious models RC4, RC5 the fixed effects \(a_i\) are replaced with club-specific effects \(a_{LL}, a_{LH}\) and \(a_{HH}\). The White heteroskedasticity correction was again necessary, and also yielded the most conservative estimates.

The coefficients for these models are reported in Table 3. The convergence coefficients are significant and have the expected sign in the single and in the strict and lax three club models. Convergence is fastest in the LL group, next fastest in the larger HH group and slower in the LH group, which can be expected since its transition may occur over different periods for different countries. The time coefficients have the correct sign in these models but are mostly insignificant. The convergence coefficients of the ‘parsimonious’ models RC4 and RC5 exhibit bias that is corrected in the fixed effects models. Their time coefficients are insignificant or have the wrong sign.

An F-test comparing the single with the strict and lax three club models finds that the inclusion of club-specific coefficients is significant at the 0.05076 and 0.00006 levels respectively (see Table 4 for the F-tests). However, comparison of the strict and the lax models finds that the additional variables are not jointly significant, because only one of the club-specific coefficients for the time terms is significant. Thus there is good evidence
that switching from the single to the three club specification is significant, but the time
term specification, which is related to the ‘technology corrected life expectancy’ concept is
not as well specified as might be desired. To find out whether club-specific fixed effects
could sufficiently describe the country fixed effects the ‘parsimonious’ models RC4 and
RC5 were estimated. However in these models the time effect does not obtain the expected
sign or is insignificant and the convergence coefficients appear to be biased. F-tests show
that the fixed effects are jointly significant. The strict three club model is therefore the best
of models RC1 to RC5.

The fixed effects ai represent growth effects arising from the technological term ϕg and the
steady state level v0. Figures 8.3 and 8.4 scatter plot the displaced and rescaled fixed
effects ai, in the form (ai–mean(ai))/βclub(i), against initial life expectancy. For each club this
expression of ai is a measure of each country’s life expectancy steady state level, expressed
relative to the club’s mean steady state level (see equation 10). The positive correlation that
exists between these relative fixed effects and initial life expectancy is to be expected
because countries with better conditions for economic growth are likely to enjoy better
living standards at the initial date.

The Wald tests in Table 3 show in the case of the strict three club model that the LH
convergence coefficient is significantly different from both its LL and HH counterparts at a
confidence level better than 1 percent. The LL and HH coefficients cannot be significantly
distinguished. On the other hand it need not be surprising that these coefficients for slower
growing trajectories be similar. In the case of the lax three club model, the insignificant
time coefficients blur the distinction between the LL and HH coefficients further. However, the respective convergence coefficients are different at the 0.0431 significance
level.

According to the Durbin Watson statistics there is no significant autocorrelation of the
errors along time. Hence that the model is a first order system is not a significant
limitation, a question that the persistency of health and health improvements could pose.

The finding that life expectancy dynamics are club-specific is quite robust. Both in the
regressions shown here and in other estimates performed during the course of this study
(with and without the White correction, the AR(1) terms and fixed effects), the F tests
consistently show the strict three club model to be significantly better than its alternatives,
and the Wald tests consistently show that most of the sets of coefficients describing each
group of countries are significantly different. The multiple peak structure is also only
explained by the three club models.

4. Conclusions

The econometric tests show that both the levels and relative convergence of life expectancy
trajectories are better described as club-specific then as single-club phenomena. The
statistical analysis thus confirms what is evident to the eye in the sequence of histograms
(Figure 1), and which is confirmed by the location of mean life expectancy by subsamples
(Figure 2). A single-club description of levels or of convergence properties of life
expectancy dynamics proves to be misspecified, and a study of the averages yields little
insight of the processes occurring within each club. Moreover, such a description cannot
explain the multiple-peaked nature of the data. As we discussed above, there is no evident
exogenous reason, including population growth rates, for multiple peakedness. The three subsamples that were defined each follow quite different trajectories, yet enjoy the property of relative convergence, with parameters differing between them. The tests that were conducted give strong evidence that large-scale life expectancy and therefore economic growth convergence clubs exist. It is clear that the methods used cannot yield a firm categorization of countries. Indeed it is quite possible that a further subdivision of the clubs would correspond closer to reality. Especially the HH group may contain further clubs, a subdivision that was not attempted.

The characteristics of the three groups of countries roughly correspond with the convergence club typology that the Howitt and Mayer-Foulkes (2001) model suggests. The life expectancy of the LL countries is consistent with stagnating economies whose technological change consists of implementation that requires very little and almost costless innovation. The life expectancy improvement of LH countries, on the other hand, requires the implementation of a series of technologies. The HH group contains those countries carrying out R&D, but also contains many countries that only implement technology. As was mentioned, it can probably be subdivided into an R&D and an implementation convergence club. On the other hand, the club structure in life expectancy dynamics may also be due to health-specific poverty traps. Examples would be a low-income trap explained by efficiency wages, of by persistent educational inequality as in Galor and Mayer-Foulkes (2002).

It is much harder to detect convergence clubs in the income data. In this sense the life expectancy data are special in that the club structure is much more evident, and can be detected with simpler econometric methods. Life expectancy has technological requirements that cannot be eluded and may provide a better indication of technological development than income, which can result from highly specialized production, and therefore may give only a poor reflection of the state of technological development.

We have shown that life expectancy can be modeled in terms of the underlying economic variables (capital and technology). The dynamics of these variables are in turn described by the theories of economic growth. Generically any steady state in any model will give rise to a steady-state-specific convergence equation that we have tested. Thus the descriptive properties of life expectancy dynamics provide a qualitative test of these theories, giving strong evidence that only theories implying convergence clubs can be valid. Such theories can explain the nature of the economic processes leading to multiple steady states and giving rise to convergence clubs, and lead to an understanding of states of development. Examples of such explanation could be the type of technological innovation taking place, or health-related poverty traps.

The existence of convergence clubs implies that countries may remain trapped in their state of underdevelopment if only market policies are followed. This holds even more strongly for convergence clubs in health, an indicator of the human development that is essential for productivity growth. Perhaps this is one reason why market policies for globalization and growth have not been as effective as hoped for in the case of underdeveloped countries. Only the recognition and careful study of multiple steady states and convergence club dynamics can lead to policies that can aim at escaping poverty traps and changing states of development.
References


## Appendix

### Table 1
Composition of the three subsamples by regions

<table>
<thead>
<tr>
<th>Subsample</th>
<th>East Asia Pacific</th>
<th>Sub Saharan Africa</th>
<th>Latin America and Caribbean</th>
<th>Europe and North America</th>
<th>Middle East, North Africa and South Asia</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>Low-Low</td>
<td>2</td>
<td>35</td>
<td>1</td>
<td>0</td>
<td>2</td>
<td>40</td>
</tr>
<tr>
<td>Low-High</td>
<td>8</td>
<td>10</td>
<td>8</td>
<td>1</td>
<td>15</td>
<td>42</td>
</tr>
<tr>
<td>High-High</td>
<td>13</td>
<td>2</td>
<td>21</td>
<td>38</td>
<td>7</td>
<td>81</td>
</tr>
<tr>
<td>Total</td>
<td>23</td>
<td>47</td>
<td>30</td>
<td>39</td>
<td>24</td>
<td>163</td>
</tr>
</tbody>
</table>

Source: author
Table 2
Level models for life expectancy dynamics

<table>
<thead>
<tr>
<th>Model</th>
<th>L1</th>
<th>L2</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Single Club</td>
<td>Three Club</td>
</tr>
<tr>
<td>TIME</td>
<td>0.091 (4.637)</td>
<td></td>
</tr>
<tr>
<td>TIME2</td>
<td>-0.005 (-4.16)</td>
<td></td>
</tr>
<tr>
<td>LL*TIME</td>
<td></td>
<td>0.112 (3.035)</td>
</tr>
<tr>
<td>LL*TIME2</td>
<td></td>
<td>-0.007 (-2.763)</td>
</tr>
<tr>
<td>LH*TIME</td>
<td></td>
<td>0.099 (5.031)</td>
</tr>
<tr>
<td>LH*TIME2</td>
<td></td>
<td>-0.005 (-3.785)</td>
</tr>
<tr>
<td>HH*TIME</td>
<td></td>
<td>0.044 (5.411)</td>
</tr>
<tr>
<td>HH*TIME2</td>
<td></td>
<td>-0.002 (-4.726)</td>
</tr>
<tr>
<td>AR(1)</td>
<td>0.773 (36.587)</td>
<td>0.695 (8.463)</td>
</tr>
<tr>
<td>Durbin-Watson</td>
<td>2.16</td>
<td>2.104</td>
</tr>
<tr>
<td>F-statistic</td>
<td>27966</td>
<td>9679</td>
</tr>
<tr>
<td>Probability</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>R-squared</td>
<td>0.983</td>
<td>0.984</td>
</tr>
<tr>
<td>Adjusted R-sq</td>
<td>0.98</td>
<td>0.981</td>
</tr>
</tbody>
</table>

Wald tests of equality for subsample coefficients

<p>| | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>LL = LH</td>
<td>9.302</td>
<td>(0)</td>
</tr>
<tr>
<td>LH = HH</td>
<td>1.834</td>
<td>(0.16)</td>
</tr>
<tr>
<td>LL = HH</td>
<td>33.45</td>
<td>(0)</td>
</tr>
</tbody>
</table>

Source: author
Note: Coefficients shown with t statistics in parenthesis. Wald tests show F statistic with probability in parenthesis
### Table 3
Relative convergence models for life expectancy dynamics

<table>
<thead>
<tr>
<th>Model</th>
<th>RC1</th>
<th>RC2</th>
<th>RC3</th>
<th>RC4</th>
<th>RC5</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Single Club</td>
<td>Strict Three Club</td>
<td>Lax Three Club</td>
<td>Parsimonious Strict Three Club</td>
<td>Parsimonious Lax Three Club</td>
</tr>
<tr>
<td>TIME</td>
<td>0.00047 (1.307)</td>
<td>0.00056 (1.547)</td>
<td>-0.00024 (-1.841)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>LOG(LE)</td>
<td>-0.04263 (-3.818)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>LL</td>
<td></td>
<td></td>
<td>0.12074 (4.327)</td>
<td>0.11297 (3.338)</td>
<td></td>
</tr>
<tr>
<td>LL*TIME</td>
<td></td>
<td></td>
<td>0.00084 (0.852)</td>
<td></td>
<td>-0.00051 (-1.145)</td>
</tr>
<tr>
<td>LL*LOG(LE)</td>
<td></td>
<td></td>
<td>-0.0623 (-3.838)</td>
<td>-0.06764 (-2.515)</td>
<td>-0.03013 (-4.058)</td>
</tr>
<tr>
<td>LH</td>
<td></td>
<td></td>
<td></td>
<td>0.05706 (6.936)</td>
<td>0.04221 (4.524)</td>
</tr>
<tr>
<td>LH*TIME</td>
<td></td>
<td></td>
<td>0.00062 (1.14)</td>
<td></td>
<td>-0.00061 (-3.402)</td>
</tr>
<tr>
<td>LH*LOG(LE)</td>
<td></td>
<td></td>
<td>-0.03124 (-4.39)</td>
<td>-0.0324 (-3.028)</td>
<td>-0.01172 (-3.096)</td>
</tr>
<tr>
<td>HH</td>
<td></td>
<td></td>
<td></td>
<td>0.0925 (8.453)</td>
<td>0.10898 (12.715)</td>
</tr>
<tr>
<td>HH*TIME</td>
<td></td>
<td></td>
<td>0.00038 (3.861)</td>
<td></td>
<td>0.00002 (0.223)</td>
</tr>
<tr>
<td>HH*LOG(LE)</td>
<td></td>
<td></td>
<td>-0.04984 (-3.766)</td>
<td>-0.0436 (-8.908)</td>
<td>-0.02072 (-7.75)</td>
</tr>
<tr>
<td>Durbin-Watson</td>
<td>2.152</td>
<td>2.073</td>
<td>2.04</td>
<td>1.939</td>
<td>1.967</td>
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<tr>
<td>F-statistic</td>
<td>555.5</td>
<td>203.4</td>
<td>122.3</td>
<td>63.1</td>
<td>48.3</td>
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<tr>
<td>Probability</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>R-squared</td>
<td>0.365</td>
<td>0.387</td>
<td>0.388</td>
<td>0.252</td>
<td>0.256</td>
</tr>
<tr>
<td>Adjusted R-sq</td>
<td>0.257</td>
<td>0.282</td>
<td>0.281</td>
<td>0.248</td>
<td>0.251</td>
</tr>
</tbody>
</table>

Wald tests of equality for subsample coefficients

| LL = LH         | 7.773 (0.00539) | 5.555 (0.00397) | 43.197 (0) | 19.751 (0) |
| LH = HH         | 2.048 (0.15267) | 1.102 (0.33244) | 20.384 (0) | 23.619 (0) |
| LL = HH         | 7.187 (0.00745) | 8.845 (0.00015) | 13.536 (0) | 12.674 (0) |

Source: author
Note: Coefficients shown with t statistics in parenthesis. Wald tests show F statistic with probability in parenthesis
<table>
<thead>
<tr>
<th>To:</th>
<th>From:</th>
<th>Single Club</th>
<th>Strict Three Club</th>
<th>Parsimonius Strict Three Club</th>
<th>Parsimonius Lax Three Club</th>
</tr>
</thead>
<tbody>
<tr>
<td>Strict Three Club</td>
<td>2.989</td>
<td>(0.05076)</td>
<td>1.555</td>
<td>(0.00004)</td>
<td></td>
</tr>
<tr>
<td>Lax Three Club</td>
<td>6.255</td>
<td>(0.00006)</td>
<td>0.193</td>
<td>(0.82434)</td>
<td>1.516</td>
</tr>
</tbody>
</table>

Source: author

Note: F statistic, probability in parenthesis